

**COMMUNITY UNIT SCHOOL DISTRICT 200  
ESSENTIAL LEARNINGS- MATH/GIFTED PROGRAM  
GRADE 3**

**THIRD GRADE**

**Subject expectation 1:**                    **Students will be able to demonstrate and apply an understanding of numbers and their operations, including meaning and relationships.**  
(State Goal 6)

Essential Learning 1 (Learning Standard A) (Learning Standard D)	Understand numbers, ways of representing numbers, relationships among numbers, and number systems
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- Critical Content**
- |              |    |   |
|--------------|----|---|
| <b>6.A.2</b> | a. | represent concretely or symbolically, compare and order <ul style="list-style-type: none"> <li>• whole numbers to one million</li> <li>• decimals to the hundredths place as related to money</li> </ul>                                    |
| <b>6.A.2</b> | b. | use the place-value structure of the base-ten number system <ul style="list-style-type: none"> <li>• identify the repeating place-value pattern (ones, tens, hundreds) within the periods</li> <li>• interpret expanded notation</li> </ul> |
| <b>6.A.2</b> | c. | find numbers less than zero by extending the number line  |
| <b>6.A.2</b> | d. | distinguish between prime and composite numbers using manipulatives   |
| <b>6.A.2</b> | e. | develop understanding of fractions as parts of unit wholes, as parts of a collection and as locations on number lines   |
| <b>6.D.2</b> |    |   |

Essential Learning 2 (Learning Standard B)	Understand meanings of operations and how they relate to one another
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- Critical Content**
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|----------------|----|--|
| <b>6.B.2</b>   | a. | create representations that show the various meanings of multiplication and division of whole numbers including partial products <ul style="list-style-type: none"> <li>• equal groups</li> <li>• arrays</li> <li>• area of rectangles</li> </ul>  |
| <b>6.B.3a*</b> |    |  |
| <b>6.B.2</b>   | b. | identify and demonstrate relationships between operations using manipulatives <ul style="list-style-type: none"> <li>• division as the inverse of multiplication</li> <li>• the model of multiplication as repeated addition</li> <li>• compare two models of division including fair share division and repeated subtraction</li> </ul> |
| <b>6.B.3b*</b> |    |  |
| <b>6.C.2a</b>  | c. | apply operations and number properties including commutative, associative, distributive, equality and use them to compute with whole numbers   |
| <b>6.B.3c*</b> |    |  |
| <b>6.B.2</b>   | d. | recognize and use zero property in multiplication  |
| <b>6.C.2a</b>  | e. | apply the appropriate operation to a real situation  |
| <b>6.C.2b</b>  | f. | describe a real situation in which multiplication and division are used and explain its solution   |

Essential Learning 3  
(Learning Standard C)

Compute fluently and make reasonable estimates

- Critical Content**    **6.B.2**            a. demonstrate automatic recall of basic facts through nine
- addition
  - subtraction
  - multiplication
- 6.C.2b**            b. develop and use strategies to estimate the results of whole number computations and to judge the reasonableness of such results
- use rounding to make estimations
- 6.B.2**            c. demonstrate fluency with basic number operations
- \***
- addition with *three* \* or more addends with and without regrouping
  - addition and subtraction with two or three digits with and without regrouping
  - multiplication up to one digit times two digits
  - addition and subtraction of decimals noted as money

Essential Learning 4 \*

Choose appropriate technology/tools

- Critical Content**    \*
- a. select appropriate methods and tools, according to the context, for computing
- mental computation
  - estimation
  - calculators
  - and paper and pencil

Essential Learning 5 \*

Recognize the connections between number sense and other math strands

**Critical Content**

Essential Learning 6 \*

Construct and communicate convincing arguments

- Critical Content**    \*
- a. demonstrate correct usage of the language related to number sense, product, factors, rounding, regrouping, expanded notation, digit vs. number, face value vs. place-value, zero property, equality
- \*
- b. make and test conjectures and form generalizations about number sense
- the larger the divisor, the smaller the quotient and vice versa
- 6.C.2b**            c. show evidence that computational results using whole numbers are correct and/or that estimates are reasonable

**THIRD GRADE:**

**Subject Expectation 2  
(State Goal 7)**

**The student will be able to estimate, make and use measurements of objects, quantities and relationships and determine acceptable levels of accuracy.**

Essential Learning 1 (Learning Standard A)	Understand measurable attributes of objects and the units, systems, and process of measurement
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- Critical Content**
- 7.A.2a**
    - a. recognize the measurable attribute
      - geometric attributes: length, area and volume
        - estimate, compare and measure length, width, perimeter and area of shapes
        - determine the number of cubes needed to fill a variety of rectangular solids
  - 7.A.3a\***
    - capacity
      - compare two or more containers in terms of their capacities including ounce, cups, pints, quarts, gallons, milliliters and liters
  - 7.A.2a**
    - weight/mass
      - compare two or more objects according to weight (mass) including ounce, pound and ton
  - 7.A.3b\***
    - temperature
      - understand degrees Fahrenheit and Celsius as a unit of measure
  - 7.A.2b**
    - money
      - find equivalent collections of coins
      - use decimals and symbols to appropriately represent money
  - \***
  - 7.A.3b\***
    - time
      - identify and order months of the year/days of the week
      - measure time in days, weeks, months, years, decades and centuries
      - read and write digital time
      - read and illustrate time on an analog clock to one minute intervals
      - estimate the passage of time
      - construct a time line
  - 7.A.2a**
    - b. compare and order objects
  - 7.A.2a**
    - c. use non-standard\* and standard measurements
  - 7.A.3b\***
    - d. recognize and apply appropriate benchmarks for an attribute *such as* the boiling point or freezing point, right angle and half past the hour
  - 7.B.3\***
    - e. select appropriate unit or tools for the attribute being measured
  - 7.A.3b\***
    - f. explore the value of measuring with standard units: customary and metric
  - 7.A.2a**
    - g. compare the relationships among the various units within a system
  - 7.A.2a**
    - h. compute simple unit conversions within a system of measurement, *such as* centimeter to meter

Essential Learning 2  
(Learning Standard B)  
(Learning Standard C)

Apply appropriate techniques, tools and formulas to determine measurements

- Critical Content** 7.B.3\*  
7.B.3\*
- a. select appropriate units and tools for the attribute to be measured
  - b. demonstrate an accurate use of tools to determine measurement
    - geometric attributes
      - ruler, yardstick, meter stick, trundle wheel and tape measure
    - capacity
      - graduated cylinders, various containers
    - weight/mass
      - balance, customary scale
    - temperature
      - variety of thermometers
    - money
      - money manipulatives
    - time
      - calendar, digital clock, analog clock
  - c. develop and use strategies for finding area, perimeter of rectangles and squares culminating in the *determination of appropriate formulas*\*
- 9.C.2  
7.A.4b\*

Essential Learning 3 \*

Recognize the connections between measurement and other math strands

**Critical Content**

Essential Learning 4 \* Construct and communicate convincing arguments and proofs to solve problems

- Critical Content** \*
- a. defend the value of measuring with standard units in customary and metric systems
  - b. make and test conjectures about measurement properties and relationships *such as*
    - form generalization that the smaller the unit, the more you need and vice versa
    - recognize the transitive relationship in ordering objects according to some attribute *such as*  $a > b$  and  $b > c$  leads to  $a > c$
  - c. demonstrate correct usage of the language related to measurement
  - d. develop logical arguments to justify conclusions about topics *such as* formulas for perimeter and area

### THIRD GRADE

**Subject Expectation 3**  
(State Goal 8)

**The student will be able to use algebraic and analytical methods to identify and describe patterns and relationships in data, solve problems and predict results.**

Essential Learning 1 (Learning Standard A) (Learning Standard B)	Understand patterns, relations, and functions
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- Critical Content**
- 8.A.2a** a. describe, extend and create geometric and numeric patterns
  - 8.A.2a** b. represent and analyze patterns and functions using words, tables and graphs
  - 8.A.2a** c. relate and compare different forms of representation for a relationship
  - 8.B.2** d. analyze a geometric pattern and express the results numerically

Essential Learning 2 (Learning Standard C)	Represent and analyze mathematical situations and structures using algebraic symbols
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- Critical Content**
- 8.C.2** a. explain operations and number properties including commutative, associative, distributive, equality and use them to compute with whole numbers
  - 8.A.2b** b. construct and solve number sentences using a variable to represent an unknown quantity
  - \*** c. express mathematical relationships *using equations\**

Essential Learning 3 (Learning Standard D)	Use mathematical models to represent and understand quantitative relationships and solve problems
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- Critical Content**
- 8.D.3a\*** a. model and solve real life problems using various representations including (but not limited to) objects, graphs and tables

Essential Learning 4 *	Use problem solving to analyze change in real life situations
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- Critical Content**
- \*** a. investigate how a change in one variable relates to a change in a second variable using objects, tables and graphs
  - \*** b. identify and describe situations with constant rates of change and compare them
  - 8.D.2** c. solve linear equations involving whole numbers in real life situations

Essential Learning 5 *	Choose appropriate technology/tools for algebraic representation
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- Critical Content** \*
- a. use manipulatives, *such as* Algebra Tiles, Hands On Equations, etc., to solve linear equations

Essential Learning 6 *	Recognize the connections between algebra and other math strands
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- Critical Content** \*
- \* a. apply the commutative and associative properties for addition
  - \* b. apply the commutative property for multiplication
  - \* c. explore the associative property for multiplication
  - \* d. use opposite operations to find missing numbers in equations
  - \* e. observe patterns in our environment, *such as* Fibonacci numbers
  - \* f. find, describe, extend and create patterns using manipulatives/numbers/letters/hundreds charts/arrays with an emphasis on number sense)
  - \* g. find, describe, extend and create geometric patterns using tessellations
  - \* h. recognize patterns of odd/even numbers

Essential Learning 7 *	Construct and communicate convincing arguments and proofs to solve problems
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- Critical Content** \*
- \* a. demonstrate correct usage of the language related to algebra, including constants, variables, commutative, associative, distributive, and equality
  - \* b. demonstrate correct usage of the language related to patterns including skip counting
  - \* c. develop logical arguments to justify conclusions about topics *such as* unknown quantities
  - \* d. identify the rule used to generate a pattern
  - \* e. make and test conjectures about algebra properties as seen in the patterns developed

**THIRD GRADE:**

**Subject expectation 4  
(State Goal 9)**

**The student will use geometric methods to analyze, categorize and draw conclusions about points, lines, planes and space.**

Essential Learning 1 (Learning Standard A) (Learning Standard B)	Analyze characteristics and properties of two- and three-dimensional geometric shapes and develop mathematical arguments about geometric relationships
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- Critical Content**
- 9.A.1a** a. identify, compare, order *and analyze*\* attributes of regular and non-regular polygons (convex and non-convex) and circles/ellipses up to 12-sided figures
  - 9.B.2** \*
  - 9.A.1a** b. identify, compare, order and *analyze*\* attributes of 3-dimensional figures including sphere/cone/cylinder/pyramid/rectangular prism
  - 9.B.2 & \*** c. explore concepts of congruence and similarity
  - 9.B.2** d. develop and use vocabulary to describe attributes of 2-dimensional figures including angles, sides, vertices
  - \*** e. develop and use vocabulary to describe attributes of 3-dimensional shapes including faces, vertices, edges
  - \*** f. recognize shapes that do and do not tessellate

Essential Learning 2 *	Specify locations and describe spatial relationships using coordinate geometry and (or) other representational systems
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- Critical Content**
- \*** a. make and use coordinate systems to specify locations and to describe paths
  - \*** b. make representations of polygons using tools *such as* geoboards, dot paper, power blocks, grid paper and pattern blocks

Essential Learning 3 (Learning Standard C)	Use visualization, spatial reasoning and geometric modeling to solve problems
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- Critical Content**
- \*** a. examine polygons to determine whether or not they can be put into patterns without gaps and overlaps (tessellate)

Essential Learning 4 *	Apply transformations and use symmetry to analyze mathematical situations
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- Critical Content**
- 9.A.3b\*** a. transform it into shapes that will tessellate
  - \*** b. predict and describe results of sliding, flipping, and turning 2-dimensional shapes
  - 9.A.3c\*** c. identify and describe line symmetry in 2-dimensional shapes and designs
  - 9.A.3c\*** d. identify and describe rotational symmetry in 2-dimensional shapes and designs

Essential Learning 5 *	Recognize the connections between geometry and other math strands
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**Critical Content** \* a. construct models showing connections between geometry and square and triangular numbers

Essential Learning 6 (Learning Standard C)	Construct convincing arguments and proofs to solve problems
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**Critical Content** 9.C.2 a. make and test conjectures about geometric properties and relationships and develop logical arguments to justify conclusions

### THIRD GRADE

**Subject Expectation 5**  
(State Goal 10)

**The student will select, organize and analyze data using statistical methods; predict results; and interpret uncertainty using concepts of probability.**

Essential Learning 1 (Learning Standard A) (Learning Standard B)	Develop concepts of data collection and analysis
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**Critical Content**

- 10.B 2a**
  - 10.B.2b**
  - 10.B.2b**
  - 10.B.2c**
  - 10.B.2d**
  - 10.B.2d**
  - 10.A.2b**
  - 10.A.2b**
  - 10.B.2d**
  - 10.A.3a\***
  - 10.A.2c**
- a. use the steps to solve for problems
    - identify the problem (question)
    - collect/gather data
    - organize and display the data
    - analyze the data
    - make and test conjectures about data
    - draw conclusions
  - b. develop strategies using manipulatives to determine mean, median and mode
  - c. identify mean, median, mode and range using a data set (given or collected)
  - d. read and interpret data represented on a tally chart, a bar graph, a circle graph, a line plot, a pictograph, a line graph and a stem and leaf plot
  - e. display and analyze data using line plots, bar graphs and circle graphs
  - f. move from noticing individual features of the data to describing the overall shape of the data distribution
  - g. make predictions and decisions based on data and communicate their reasoning

Essential Learning 2 (Learning Standard C)	Develop the concept of probability
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- Critical Content**
- 10.C.2d**
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  - 10.C.2b**
  - 10.C.2b**
  - 10.C.1b**
- a. explore experimental probability through a series of data collection experiments (simple events) that are recorded and analyzed *such as* coin toss, spinners, dice and computer games
  - b. make a connection between theoretical probability and experimental probability through repetition of each of the experiments
  - c. describe events as likely or unlikely and discuss the degree of likelihood using words, *such as* certain, equally likely and impossible
  - d. understand that the measure of the likelihood of an event can be represented by a number on a scale from 0 to 1
  - e. chart/list combinations of possible outcomes

Essential Learning 3*	Choose appropriate tools for data collection and representation
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**Critical Content 10.B.2c** a. use technology, *such as* Math Keys, to show and analyze data

Essential Learning 4*	Recognize the connections between data collection and probability and other math strands
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**Critical Content** \*  
 \* a. connect the concept of mean to fair share division  
 \* b. connect the concept of the scale of probability to ratio  
 \* c. connect number scale 0-1 to fractions

Essential Learning 5*	Construct and communicate convincing arguments and proofs to solve problems
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**Critical Content** \*  
 a. demonstrate correct usage of the language related to data collection and probability including mean, median, mode, range, cluster, gap, interval, outliers and extrapolate  
**10.A.2c** b. discuss possible outcomes of experiments  
**10.A.3c\*** c. make and test conjectures about data/probability properties and relationships *such as* different measures of central tendency reveal different aspects of data distribution  
**10.A.3c\*** d. develop logical arguments to justify conclusions about topics including the shape of data

# Math Curriculum for the Replacement Program Grades 3,4, and 5

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May 2001